

Hydraulics:

Basic principles of physics

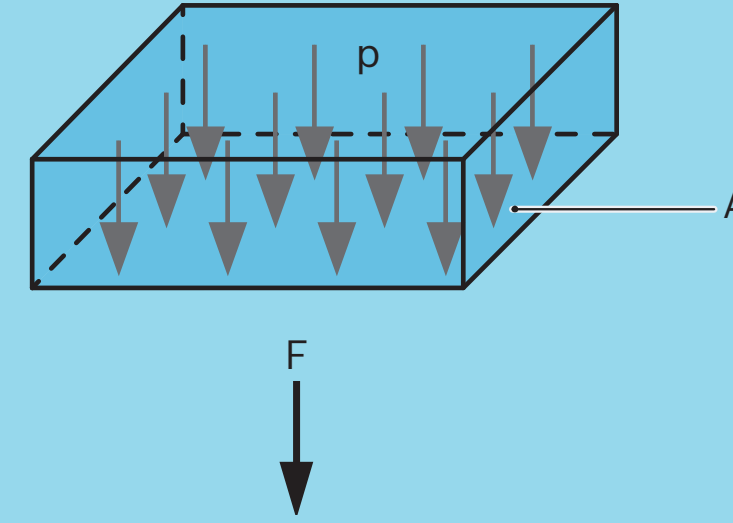
Hydrostatics - Pascal's law

1 bar = 10 N/cm²
1 bar = 10⁵ Pa
1 bar = 0,1 MPa

1 psi = 6894,757293168 Pa
1 bar = 14,49 psi

$$p = \frac{F}{A} \Rightarrow F = p \cdot A$$

$$1 \text{ Pa} = 1 \frac{\text{N}}{\text{m}^2}$$



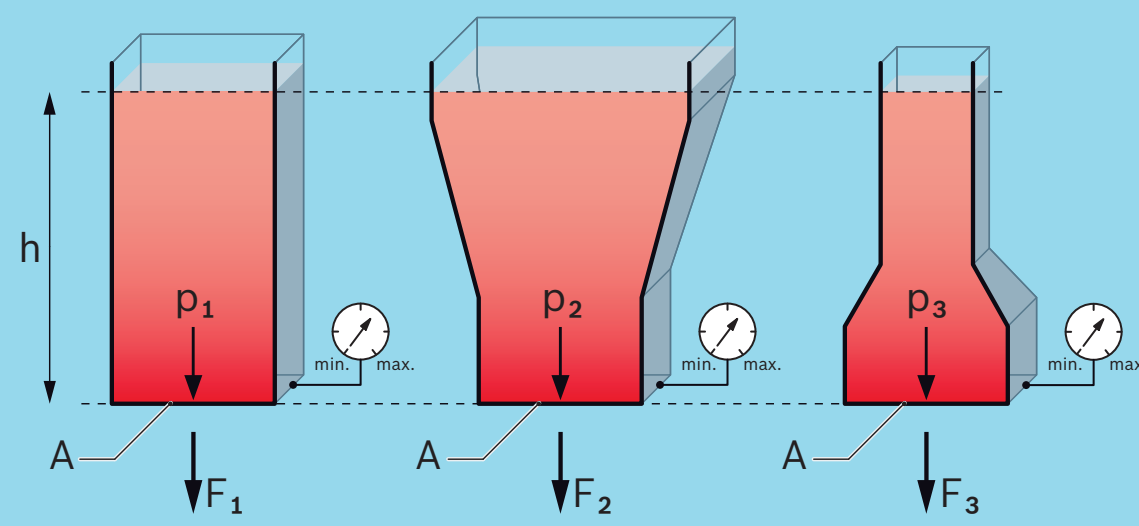
Hydrostatic pressure due to gravity

$$p = \rho \cdot g \cdot h$$

$$p_1 = p_2 = p_3$$

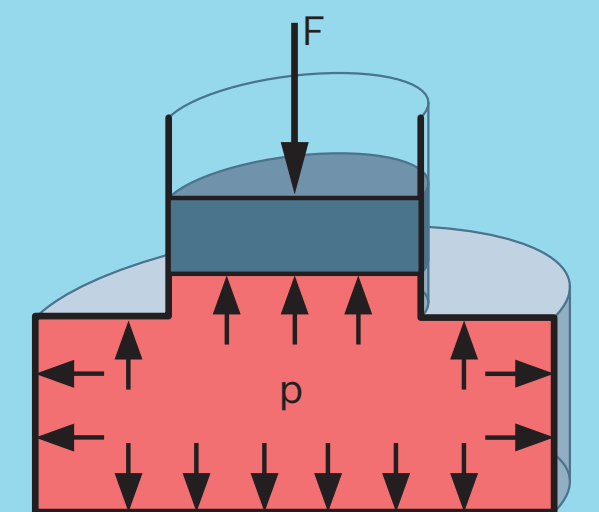
$$F_1 = F_2 = F_3$$

p Hydrostatic pressure
ρ Specific density of the fluid
g Acceleration due to gravity (9,81m/s²)
h Height of the fluid column



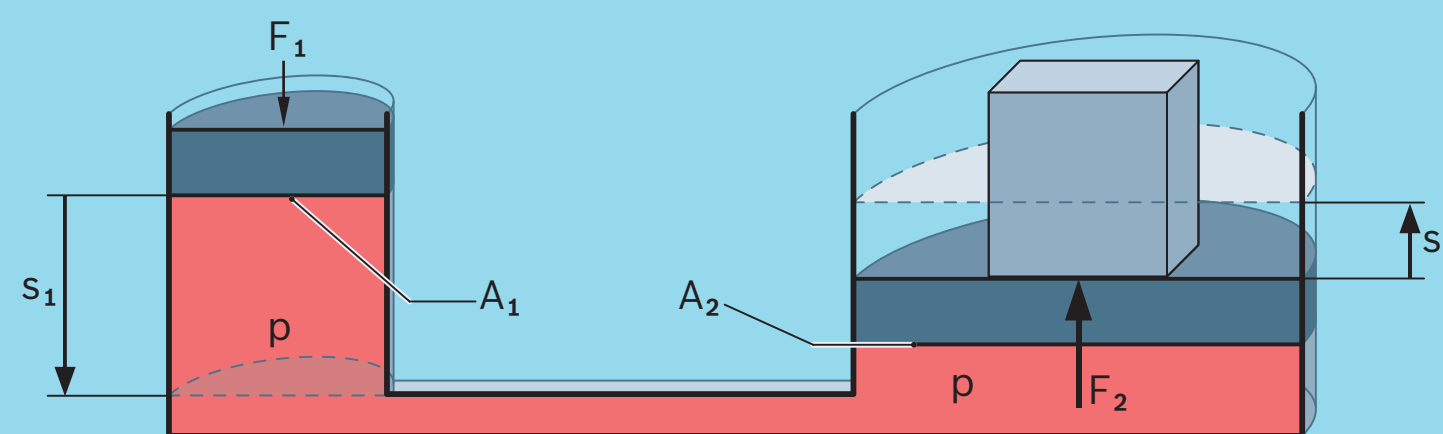
Hydrostatic pressure due to external forces

$$p = \frac{F}{A}$$



Force transmission

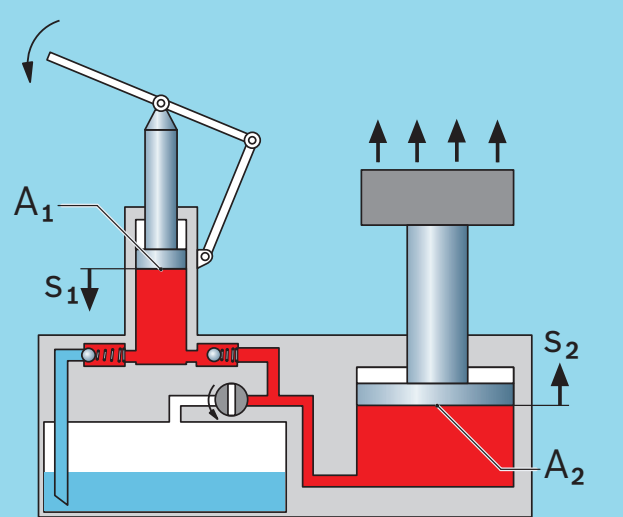
$$p = \frac{F_1}{A_1} = \frac{F_2}{A_2}$$



Hydraulic lever rule

$$\Delta V = A_1 \cdot s_1 = A_2 \cdot s_2$$

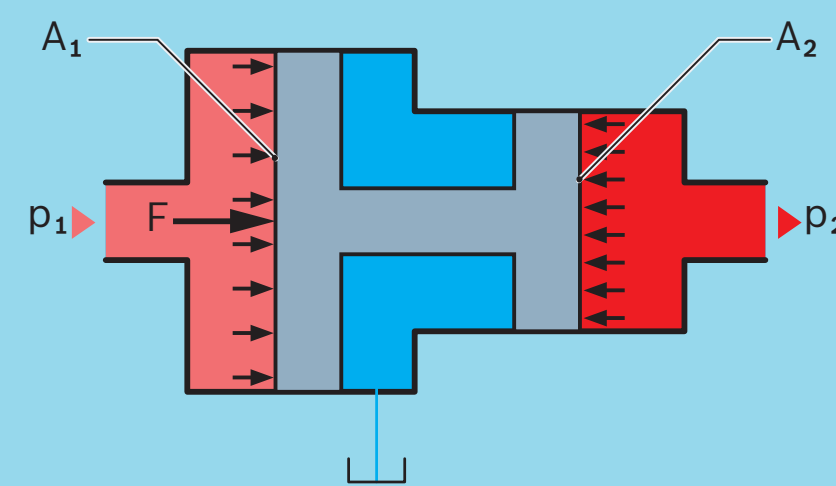
$$s_2 = s_1 \frac{A_1}{A_2}$$



Pressure intensification

$$p_1 \cdot A_1 = p_2 \cdot A_2$$

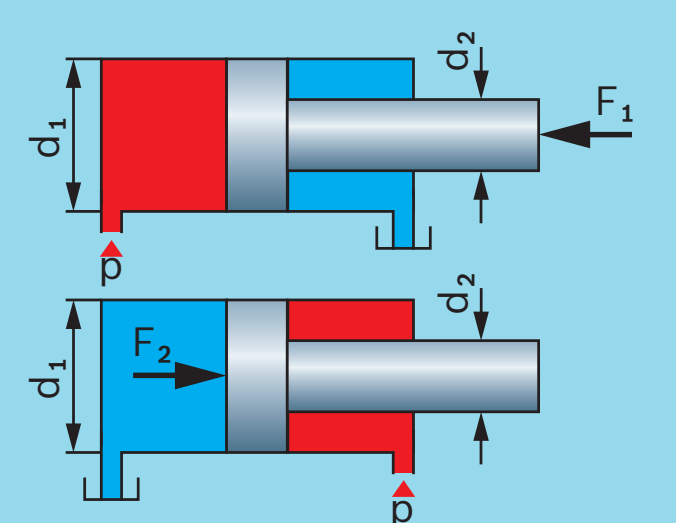
$$p_2 = p_1 \frac{A_1}{A_2}$$



Forces ratio: differential cylinder

$$F_1 = p \frac{\pi d_1^2}{4}$$

$$F_2 = p \frac{\pi (d_1^2 - d_2^2)}{4}$$

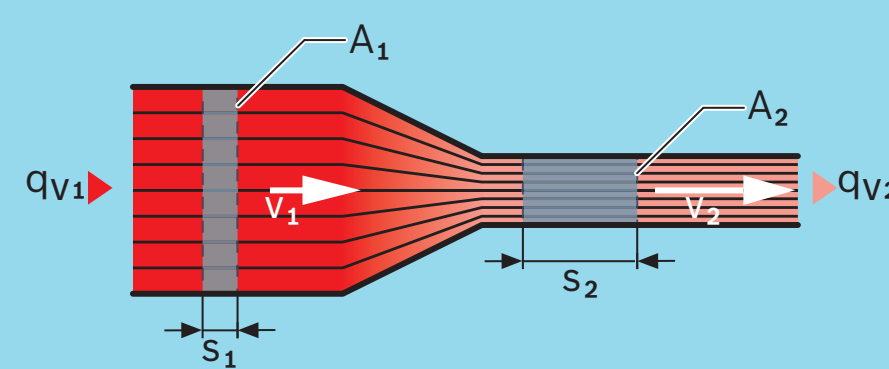


Continuity law

$$A_1 \cdot s_1 = A_2 \cdot s_2$$

$$V_1 = V_2$$

A₁, A₂ Cross-sectional areas
V₁, V₂ Flow velocity
s₁, s₂ Length
q_{v1}, q_{v2} Flow

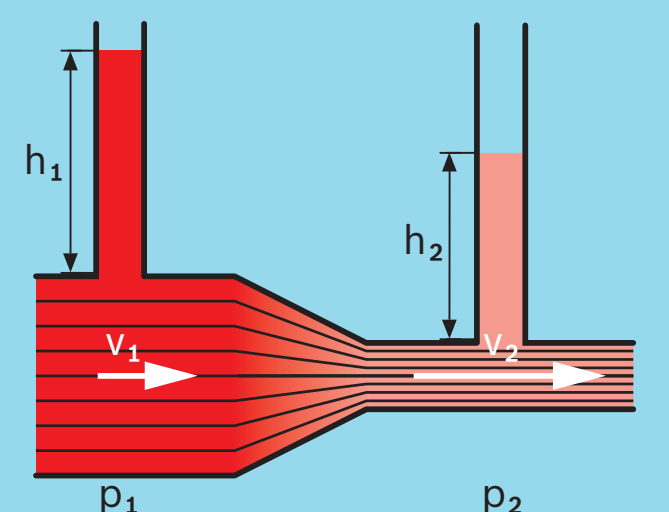


Bernoulli's Principle

$$p \cdot V + m \cdot g \cdot h + \frac{m}{2} \cdot v^2 = \text{const.}$$

$$p + \rho \cdot g \cdot h + \frac{\rho}{2} \cdot v^2 = \text{const.}$$

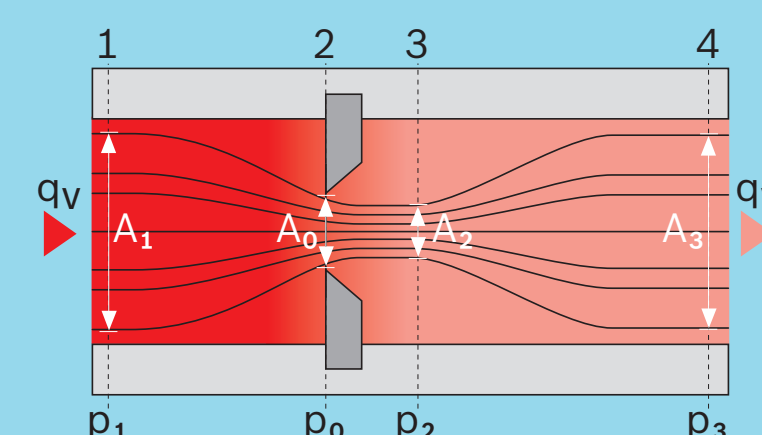
p Static pressure
ρ Specific density of the hydraulic fluid
g Acceleration due to gravity (9,81m/s²)
h Height in relation to the reference point
v Flow velocity



Orifice equation

$$q_v = \alpha_D \cdot A_0 \cdot \sqrt{\frac{2}{\rho} \cdot \Delta p}$$

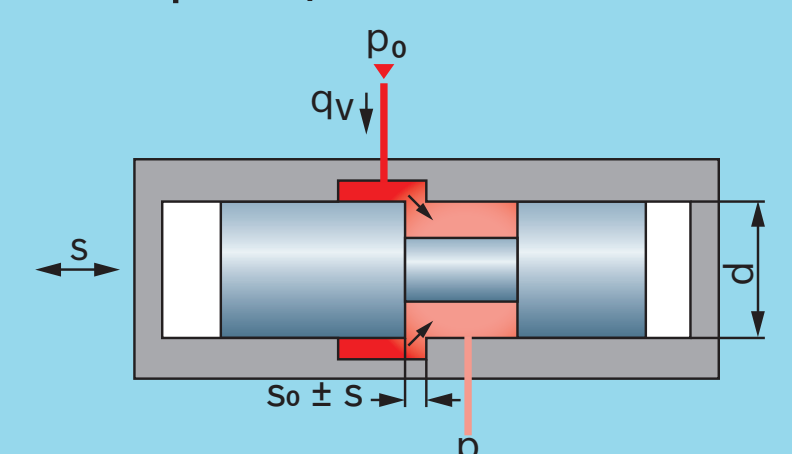
q_v Flow
A₀ Orifice cross-section
α_D Orifice contraction coefficient (orifice geometry)
ρ Hydraulic fluid density
Δp Pressure difference



Bernoulli's Principle (example: control spool)

$$q_v = (s_0 \pm s) \cdot K \sqrt{p_0 - p}$$

$$K = \alpha_D \cdot \pi \cdot d \sqrt{\frac{2}{\rho}}$$



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